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## Note

# Theoretical and practical limitations of capillary isotachophoresis in trace analysis

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The separation principle of isotachophoresis, carried out in different media (acrylamide gel, paper) can be used for qualitative and semi-quantitative analysis. Continuous free-flow isotachopohoresis is used for preparative purposes. It has been possible to carry out trace analyses since the introduction of capillary-tube isotachophoresis in the 1960s. In this paper, we shall use the term "isotachophoresis" to mean capillary-tube isotachophoresis.

The performance of any analytical technique is characterized in terms of accuracy, precision and dynamic range. In isotachophoresis the determination of the dynamic range is complicated by its dependence on the sample composition. Often associated with the dynamic range is the minimum detectable amount, which is especially important in trace analysis. Whereas in chromatography there is a common trend to use, whenever possible, more specific detectors in trace analysis, in isotachophoresis the detector sensitivity is determined by factors other than, for example, noise. Here, sensitivity is determined by the leading electrolyte concentration and the detector cell volume. Moreover, completely different interpretation is necessary to use specific detection in a more sensitive manner. The gain is a factor of 10 and not more, even in principal-component analysis.

The detection limit with universal detectors is consequently determined by both operational and equipment parameters, because zone-volumes are measured. There are a number of theoretical and practical constraints as to the operational conditions (field strength, concentration) that will be discussed. The equipment parameter (cell volume) clearly has constructional limitations, but theoretical insight has revealed that there is no point in further decreasing the cell volume because of the inherent uncertainty of the zone-volume, owing to diffusion and a number of convective disturbances from temperature gradients and electroosmosis. Evaluation of both operational and constructional limitations has shown that the absolute detection limit, that can theoretically be attained, lies 2–3 decades below that of present-day isotachophoretic equipment.

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# OPERATIONAL LIMITATIONS

The minimum detectable amount,  $q_{\min}$ , with universal detection in isotachophoresis is given by<sup>1,2</sup>:

$$q_{\min} = \pi r_0^2 lc \tag{1}$$

in which  $r_0$  is the capillary internal radius, l the detector cell length and c the separand concentration in its zone: it is clear that all three can be minimized. The separand concentration c is determined by using the Kohlrausch law, the separand mobility and the leading electrolyte composition. With a transport number of the leading electrolyte of 0.5 or greater (necessary for separation efficiency), the value of c can decrease to ca. 0.5 times that of the leading electrolyte. For reasons of a buffering capacity the latter should be in the order of  $10^{-3}$  M or more.

When minimizing the detector cell length, it should be remembered that there is an inherent uncertainty in the exact location (or moment of detection) of a zone-boundary. This uncertainty arises from three phenomena: electroosmosis, diffusion and convection due to the axial temperature gradient. In comparison with the latter the radial temperature gradient can be neglected.

Electroosmosis leads to convection of the liquid, which in turn causes an axial pressure gradient accross the zone-boundary. This gradient is zero only at distance  $r_0/\sqrt{2}$  from the capillary axis³ and gives rise to a non-planar zone-boundary. Therefore, certain precautions may be necessary: decreasing the zeta-potential of the wall, increasing the viscosity or decreasing the dielectric constant of the liquid³. The curved profile can otherwise range over a length of  $10^{-4}$  m or more.

Although diffusion in isotachophoresis is counteracted by the mechanism of self-correction, the steady-state zone-boundary composition is determined by diffusion, as described by several authors<sup>4,5</sup>.

The length of the diffusion-controlled layer is given by:

$$\Delta l_{\rm D} = 4mRT/\Delta mFE \tag{2}$$

where  $\Delta m/m$  is the relative mobility difference of the two separands. R the gas constant, T the absolute temperature, F the Faraday constant and E the average field strength. In this relation, which gives the uncertainty in the location of the zone-boundary, the diffusion coefficient, D, is included in the mobility by means of Einstein's approximation, D = mRT/F, for monovalent ions. At normal working temperatures, a mobility difference of 10% and a field strength of  $10^4$  V m<sup>-1</sup>, the diffusion length  $\Delta l_D$  is equal to  $10^{-4}$  m.

Another disturbance arises from the stepwise increase in temperature from one zone to another. The length of this disturbance can be approximated by (see ref. 3, p. 38):

$$\Delta l_{\rm C} = \rho C_{\rm p} m \Delta T / j \tag{3}$$

where  $\rho$  is the density,  $C_p$  the specific heat of the liquid,  $\Delta T$  the temperature difference and j the current density. For a separand with mobility of  $50 \cdot 10^{-9}$  m<sup>2</sup> V<sup>-1</sup> sec<sup>-1</sup> in water at  $j = 10^3$  A m<sup>-2</sup>,  $\Delta l_{\rm C}$  is  $2 \cdot 10^{-4}$  m per degree temperature difference.

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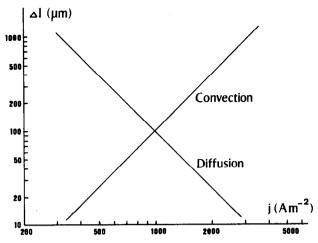


Fig. 1. The length of the convective ( $Al_{\rm C}$ ) and diffusive disturbance ( $Al_{\rm D}$ ) in isotachophoresis as a function of the current density. Conditions for this example are mentioned in the text. A capillary of 0.2 mm I.D. was used.

Zone-to-zone temperature differences were determined experimentally in capillaries with different inner diameters<sup>6</sup>. In a capillary with  $r_0 = 10^{-4}$  m and at the current density mentioned, the temperature difference amounts to  $10^{\circ}$ K between leading and terminating electrolytes. With an approximate zone-to-zone difference of  $0.5^{\circ}$ K, the length of the convective disturbance,  $\Delta l_{\rm C}$ , is  $10^{-4}$  m. When optimizing the current density in this respect, an increase would seem attractive from eqn. 3. However, experiments have shown that  $\Delta T$  is proportional to  $j^2$ . Consequently, a higher current density even increases  $\Delta l_{\rm C}$ . Alternatively, a lower current density, through E, increases  $\Delta l_{\rm D}$ . Fig. 1 illustrates these effects. It was shown that, under the conditions described  $\Delta l_{\rm D}$  and  $\Delta l_{\rm C}$  are of the same order of magnitude *i.e.* ca.  $10^{-4}$  m.

## CONSTRUCTIONAL LIMITATIONS

It was shown that operational limitations give rise to an inherent uncertainty in the zone length of  $10^{-4}$  m, so that it is unnecessary to decrease the detector cell length below this value. According to eqn. 1, the detector cell volume can also be minimized if a smaller radius is used. Several problems may arise: construction of the cell, coupling to the separation system and the danger of clogging. There is an additional fundamental limitation. The electric double-layer thickness,  $\delta$ , for dilute solutions of monovalent electrolytes at room temperature can be approximated by:

$$\delta = 0.3 \cdot 10^{-9} / \sqrt{c} \tag{4}$$

where c is the concentration (mol  $1^{-1}$ ) and  $\delta$  in metres. When  $c = 10^{-3} M$ ,  $\delta$  is  $10^{-8}$  m. With a capillary radius,  $r_0$ , of  $10^{-5}$  m, wall effects can be neglected provided that electro-osmosis is suitably accounted for. The effect of surface conductance can short-circuit the isotachophoretic process. The relative contribution of surface conductance is approximated by:

$$2\kappa^{\sigma}/r_0\kappa = 2\varepsilon^2\zeta^2/\eta\delta r_0\kappa \tag{5}$$

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where  $\kappa^{\sigma}$  is the surface conductance per unit of wall circumference,  $\kappa$  the bulk conductance,  $\varepsilon$  the dielectric constant,  $\zeta$  the zeta-potential of the wall and  $\eta$  the viscosity of the liquid. With a zeta-potential reduced to  $10^{-2}$  V, with  $\varepsilon = 80 \cdot 10^{-12}$  F m<sup>-1</sup>,  $\eta = 10^{-3}$  N m<sup>-2</sup> sec,  $\delta = 10^{-8}$  m,  $r_0 = 10^{-5}$  m and  $\kappa = 10^{-1}$  S m<sup>-1</sup>:

$$2\kappa^{\sigma}/r_0\kappa = 1.3 \cdot 10^{-7} \tag{6}$$

Under these conditions, the effect of surface conductance can indeed be neglected. A decrease of the radius of presently used capillaries from  $10^{-4}$  to  $10^{-5}$  m can consequently be considered from a theoretical point of view.

## CONCLUSIONS

The theoretical limit of detection with universal detection in isotachophoresis, given by eqn. 1, is limited by an inherent uncertainty in the zone length measured, owing to both diffusion  $(\Delta l_{\rm D})$  and convection  $(\Delta l_{\rm C})$ . The order of magnitude is  $10^{-4}$  m, with a minimum detectable zone length of  $3 \cdot 10^{-4}$  m. The double-layer thickness  $(10^{-8}$  m at  $10^{-3}$  M) should be negligible compared with the capillary radius, which in turn should be greater than  $10^{-5}$  m. The concentration in the steady state, c, should be  $10^{-3}$  M or higher.

It can therefore be concluded that the theoretical detection limit with universal detection consequently obtained amounts to  $10^{-13}$  mole for monovalent ions, or 100 femtoequivalents. This value is still 2-3 decades below that of present-day isotachophoretic equipment.

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